

Three-dimensional Computational Modeling and Simulation of Intergranular Corrosion Propagation of Stainless Steel

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In oxidizing nitric acid solutions, stainless steel undergoes intergranular corrosion accompanied by grain dropping and changes in the corrosion rate. For the safe operation of reprocessing plants, this mechanism should be understood. In this study, we constructed a three-dimensional computational model using a cellular automata method to simulate the intergranular corrosion propagation of stainless steel. The computational model was constructed of three types of cells: grain (bulk), grain boundary (GB), and solution cells. Model simulations verified the relationship between surface roughness during corrosion and dispersion of the dissolution rate of the GB. The relationship was investigated by simulation applying a constant dissolution rate and a distributed dissolution rate of the GB cells. The distribution of the dissolution rate of the GB cells was derived from the intergranular corrosion depth obtained by corrosion tests. The constant dissolution rate of the GB was derived from the average dissolution rate. Surface roughness calculated by the distributed dissolution rates of the GBs of the model was greater than the constant dissolution rates of the GBs. The cross-sectional images obtained were comparable to the corrosion test results. These results indicate that the surface roughness during corrosion is associated with the distribution of the corrosion rate.

Keywords: *Intergranular corrosion, Stainless steel, Corrosion shape, Computer simulation, Cellular automata method*

1. Introduction

In spent fuel reprocessing plant, the corrosion of the components treating oxidizing nitric acid solution such as vessels, tanks and pipes is an important issue. It is known that austenitic stainless steel in oxidizing nitric acid solution is in transpassive state showing morphology of intergranular corrosion [1]. Fig. 1 shows a cross sectional image of austenitic stainless steel stayed in transpassive state of oxidizing nitric acid. The intergranular corrosion behaviour in oxidizing nitric acid solution gives grain dropping resulting a high corrosion rate [2]. The intergranular corrosion was caused by presence of minor elements (e.g. C, P, S) in stainless steel. Especially, segregated C, P and S at GB could promote intergranular corrosion [3-6].

For safety operation of spent fuel reprocessing plants treating oxidizing nitric acid solutions, it is important to understand intergranular corrosion mechanism. For under-

standing intergranular corrosion mechanism, some researchers had developed computational model. Ohno *et al.* had developed the intergranular corrosion model considering cylindrical-shaped grains, and simulated the weight loss behaviour at the progressing intergranular corrosion [7]. Bague *et al.* had determined the penetration depth using GB dissolution model [8]. These studies showed comparable

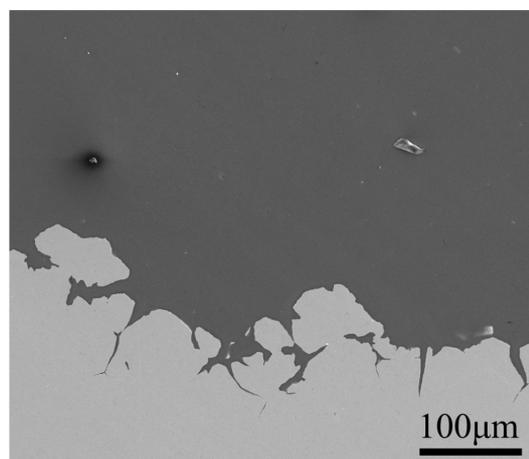


Fig. 1. Cross-sectional image of stainless steel in transpassive state

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intergranular corrosion behaviour with that obtained by intergranular corrosion tests. The effects of minor elements in stainless steel, however, was not considered in their model.

In this study, we developed three dimensional computational model using cellular automata method and conducted the simulations for intergranular corrosion behaviour of stainless steel in oxidizing nitric acid solution. In the simulations, we considered distribution of dissolution rate at GBs caused by minor elements and clarified the relation between surface roughness and dissolution rate at GBs.

2. simulation model for intergranular corrosion

In our previous study, novel two dimensional intergranular corrosion model was developed and the model suggested that various morphology of corrosion could simulate [9]. In this study, we extended our two dimensional model into three dimensional model using cellular automata method, and the simulation for intergranular corrosion was conducted using the extended model.

The cellular automata method is a discrete model which consists of a regular grid of cells, each in one of a finite number of states [10]. In this model, three dimensional space was parted into small cells. Three cells were set: interior of grain (bulk) cell, GB cell, and solution cell. The only bulk and/or GB cell contacted with solution cell corrode and change into solution cells. The shape of cell was set to rhombic dodecahedron [11] as shown in Fig. 2. The rhombic dodecahedron is a convex polyhedron with 12 congruent rhombic faces, and this tessellation can be seen as the Voronoi tessellation of the face-centered cubic lattice. Schematic example of simulation of

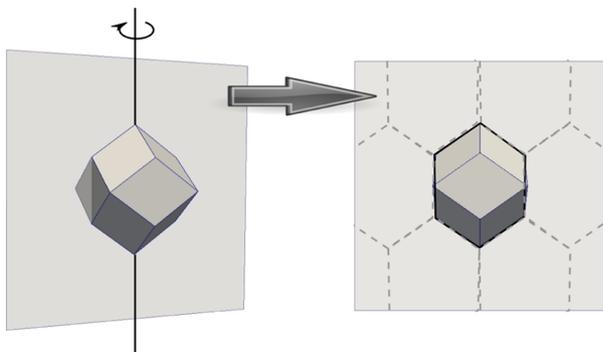


Fig. 2. Rhombic dodecahedron type cell

corrosion progress is shown in Fig. 3.

In this model, grains were composed by discrete three dimensional Voronoi diagram with wave front method [12]. The cells inside convex polyhedron and contacted with another polyhedron were bulk cells and GB cells, respectively. One of the advantages of using the discrete three dimensional Voronoi diagram and discrete cells is to give us flexibility of making various shapes of grains. The ratio of rate for changing to solution cell from bulk cell, v_{bulk} , and GB cell, v_{GB} , was defined in equation (1).

$$\frac{v_{\text{GB}}}{v_{\text{bulk}}} = \frac{(L_{\text{GB}} + L_{\text{bulk}})}{L_{\text{bulk}}} \quad (1)$$

L_{GB} and L_{bulk} are corrosion depth and penetration depth respectively as shown in Fig. 4.

Corrosion progressing length $r_{\text{bulk/GB}}$ was defined as follows:

$$r_{\text{bulk/GB}} = \sum_t v_{\text{bulk/GB}} \Delta t \quad (2)$$

where Δt represents time step of the simulation.

During the simulation, if $r_{\text{bulk/GB}}$ of each cell became larger than the length between central point of neighbored cells, r_{cell} , bulk or GB cell changed into solution cell.

$$r_{\text{bulk/GB}} > r_{\text{cell}} \quad (3)$$

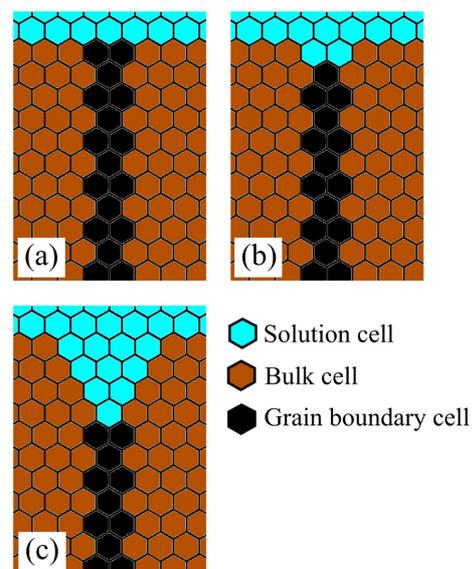


Fig. 3. Schematic example of simulation of corrosion progress; Corrosion is progressed from (a) to (c)

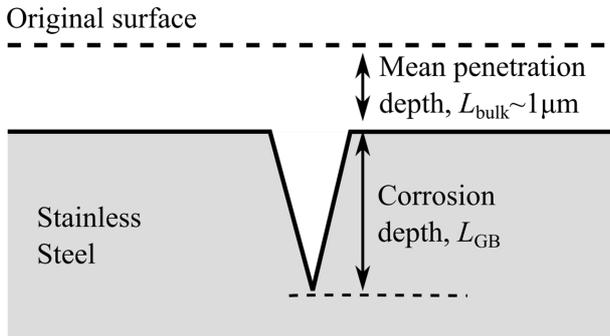


Fig. 4. Schematic view of corrosion depth

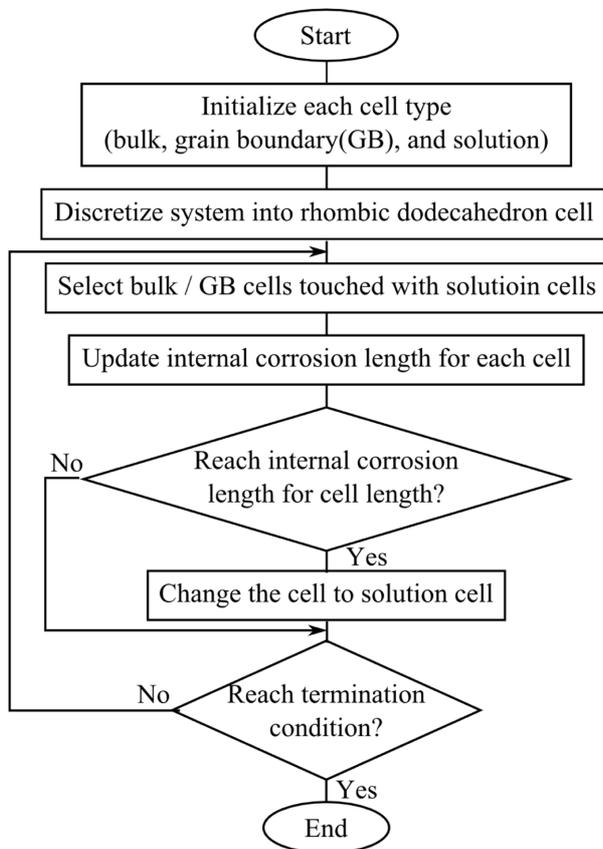


Fig. 5. Flowchart of the intergranular corrosion simulation model

In this model, the surfaces are allowed to move for Δt by changing cells using equation (2) and (3), and corrosion is represented from macroscopic viewpoint. Fig. 5 represents flowchart of the simulation model.

In this study, the simulation system was constructed by a cube of $300 \times 300 \times 300 \mu\text{m}$, and r_{cell} length was $\sqrt{2} / 2 \mu\text{m}$. The mean grain size in the simulation was $50 \mu\text{m}$

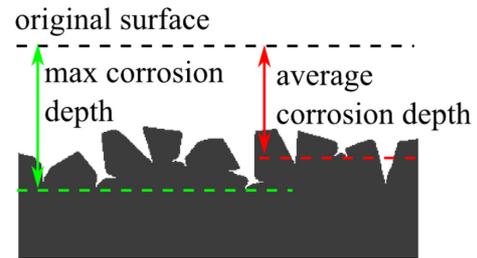


Fig. 6. Schematic view of average corrosion depth and maximum corrosion depth

by setting positions of kernel points in Voronoi tessellation. The dissolution rate of bulk cell was $2.0 \times 10^{-10} \text{ m/s}$: this was derived from experimental corrosion test [13]. Δt must be set to satisfy the Courant-Friedrichs-Lewy (CFL) condition [14]. The CFL condition is a necessary condition for stability while solving certain partial differential equations numerically.

$$\frac{r_{\text{cell}}}{\Delta t} > v_{\text{GB}} \quad (4)$$

In order to make the simulation precisely, Δt was set as follows.

$$\Delta t = \frac{r_{\text{cell}}}{10v_{\text{GB}}} \quad (5)$$

Simulation for intergranular corrosion was performed and ended over $150 \mu\text{m}$ of thinning. The average and maximum corrosion depths were analysed after the simulation. The average corrosion depth was calculated by the weight loss of the simulation system. The maximum corrosion depth was the deepest point from original surface. These corrosion depths are shown in Fig. 6. The data set was discussed in section 3. The model in this study was own program and developed by C-language. The ParaView software was used to visualize the cross-sectional and quarter view of intergranular corrosion simulation results [15].

3. data set for simulation

3.1 Distribution of intergranular corrosion rate

Data set used for simulation was the distribution of dissolution rate at GBs. This is expressed in equation (6) as a probability density function:

$$f_{\text{exp}}(x) = \alpha \exp(-\alpha x) \quad (6)$$

where α was rate parameter of the function. In this study, α was set to 0.34. This is derived from the histogram of corrosion depth of tested stainless steel as given in Fig. 7 [13]. A distribution of v_{GB} was provided by the inverse transform sampling using equation (6) [16]. The value of v_{GB} is average value which is calculated the data from our previous paper [13]. The corrosion test provided in our previous paper was presented in next subsection.

3.2 Corrosion test

3.2.1 material

One test material was Type310 stainless steel with extra high purity (Type310EHP stainless steel) [17,18]. It contains minor impurities such as C, P, S, and N: total concentration is less than 100 ppm. Other test material was Type310EHP having 270 ppm of phosphorus (Type 310-270P). It was thermal aged at 650 °C or 24 hours to segregate P at GB. Table 1 shows chemical composition of the materials.

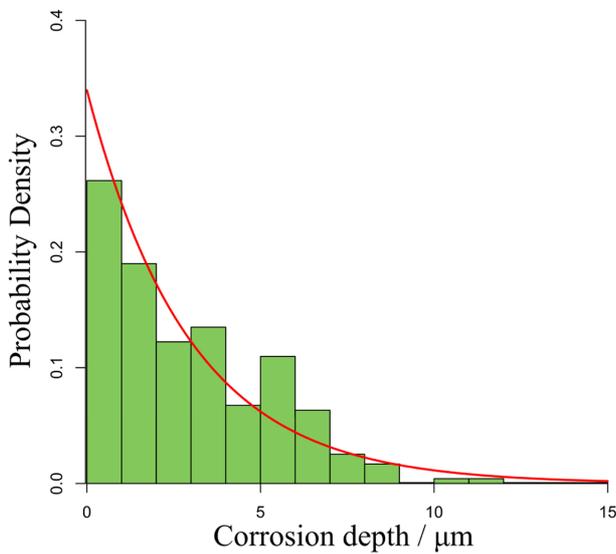


Fig. 7. Histogram of corrosion depth of Type310-270P; Red curve represents fitted curve to the exponential type function

3.2.2 corrosion test

An electrochemical corrosion test in 8M HNO₃ solution was conducted at transpassive corrosion potential [13]. The three electrode electrochemical cell was used: silver-silver chloride reference electrode (SSE), platinum plate as counter electrode, and test specimen as working electrode. The test specimen had mirror polishing finish surface. The specimen was dissolved by constant polarization at 1.1 V vs SSE. Volume of dissolved specimen was controlled by electric charge of $5 \times 10^4 \text{ C/m}^2$. In this condition, mean penetration depth L_{bulk} was about 1 μm . The corrosion depth L_{GB} was measured using cross-sectional SEM images.

4. Results and Discussion

4.1 Cross-sectional images and quarter view

Fig. 8 shows cross-sectional images of intergranular

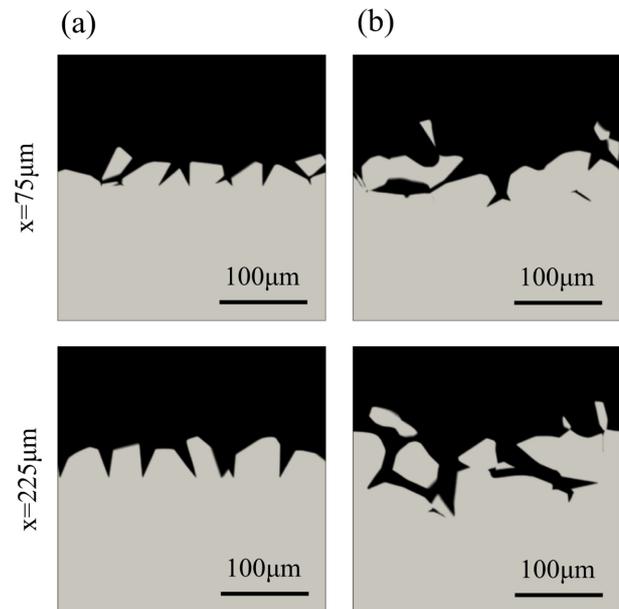


Fig. 8. Cross-sectional view of intergranular corrosion simulation on [100] plane at $x=75\mu\text{m}$ and $x=225\mu\text{m}$; (a) The simulation with constant v_{GB} . (b) The simulation with distributed v_{GB}

Table 1. Chemical compositions of specimen (mass%)

Type	C	Si	Mn	P	S	Ni	Cr	Fe
Type310 EHP	0.0011	<0.005	<0.01	0.0003	0.0008	21.2	25.9	bal.
Type310 270P	0.0063	<0.002	<0.002	0.0270	0.0009	21.0	25.8	bal.

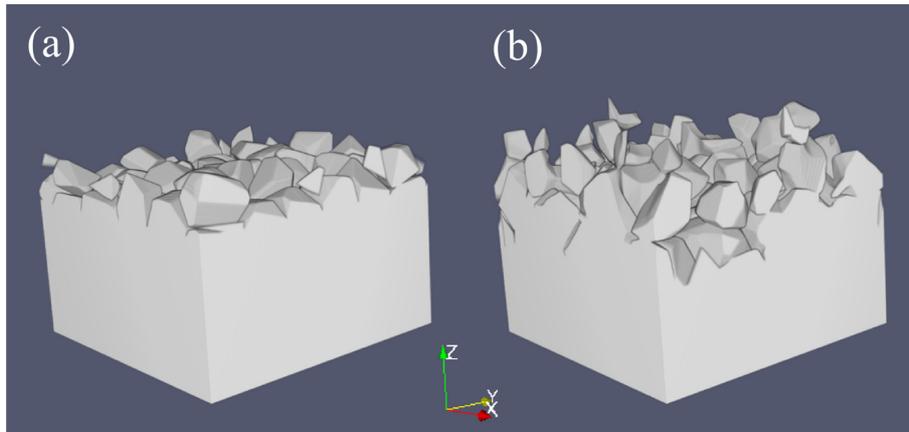


Fig. 9. Quarter views of intergranular corrosion simulation; (a) and (b) are same as Fig. 8

corrosion obtained by the simulation model. In Fig. 8a and b represent the results with constant v_{GB} and distributed v_{GB} , respectively. The simulation boxes were cut by [100] plane at $x = 75 \mu\text{m}$ and $x = 225 \mu\text{m}$. The surface roughness simulated with distributed v_{GB} was relatively larger than that with constant v_{GB} .

Fig. 9 shows the quarter view of intergranular corrosion obtained by the simulation model. In Fig. 9a and b represent same as Fig. 8. The surface roughness simulated with distributed v_{GB} was visually large compared with that simulated with constant v_{GB} .

As seen in both figures, the quarter view and cross-sectional images obtained by simulation with constant v_{GB} were rather flat compared with those in Fig. 1. On the other hand, those in cross-sectional images of the simulation with distributed v_{GB} were relatively similar with the experimental image in Fig. 1. It is thought that the difference of morphology is caused by the existence of GBs which has smaller value than average value of v_{GB} . This leads to relatively smooth surface with small grain dropping. In other words, this indicates that distribution of v_{GB} relates roughness of corroded surface.

4.2 Changes in surface area and corrosion depth during corrosion

Fig. 10 shows the relative surface areas over time. The relative surface area S_{rel} was defined as follows,

$$S_{rel} = \frac{S_{surf}}{S_{ini}} \quad (7)$$

where S_{surf} is surface area, and S_{ini} is initial area and

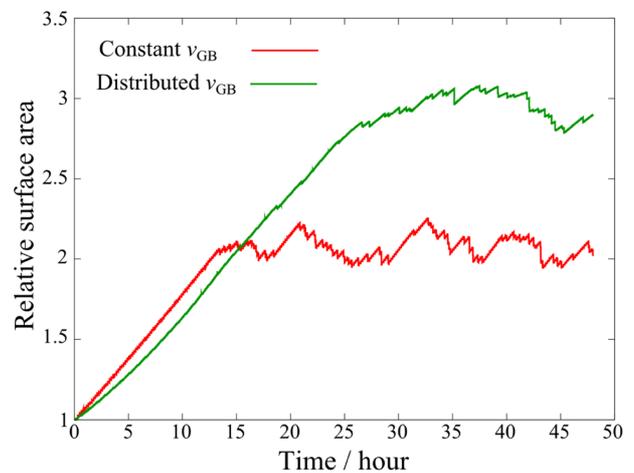


Fig. 10. Relative surface area over time

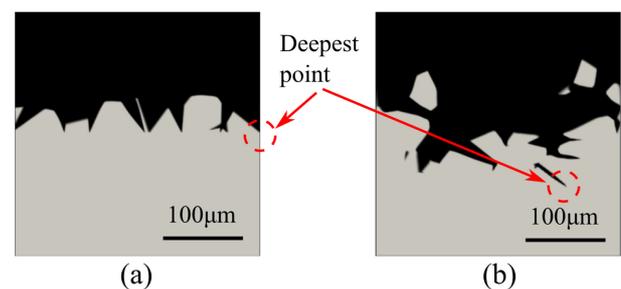


Fig. 11. Cross-sectional view of intergranular corrosion simulation on [100] plane including maximum corrosion depth. (a) and (b) are same as Fig. 8

$9.0 \times 10^4 \mu\text{m}^2$ in this simulation. The relative surface area by the simulation with distributed v_{GB} was 1.5 times larger compared with that with constant v_{GB} . This result indicates the increase of surface area occurred by remaining grains.

The cross-sectional images including maximum corrosion depth were shown in Fig. 11. Nevertheless both average corrosion depths were almost the same ($\sim 150 \mu\text{m}$), the simulation with distributed v_{GB} has corrosion depth about $70 \mu\text{m}$ deeper than that with constant v_{GB} in comparison between Fig. 11a and b. The existence of the GBs with faster dissolution rate than average value may affected the results. This indicates that the deepest point of intergranular corrosion tend to be deeper than the value expected from weight loss of specimen, and the difference is roughly $50 \mu\text{m}$ (average radius of grains) or more.

In this study, we only compared the shapes of intergranular corrosion, and did not compare the corrosion rates. However, since the simulation could reproduce the shape of intergranular corrosion of experiment could be reproduced very well, we can expect to estimate long-term intergranular corrosion using appropriate v_{bulk} and v_{GB} , which are obtained from initial stage of intergranular corrosion experiments.

5. Conclusions

In this study, three dimensional intergranular corrosion simulation of stainless steel in boiling nitric acid solution was conducted. The results were concluded as follows.

(1) Three dimensional computational model for intergranular corrosion simulation using cellular automata method was developed.

(2) Surface roughness was related to distribution of dissolution rates of grain boundaries and existence of the distribution promote surface roughness.

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